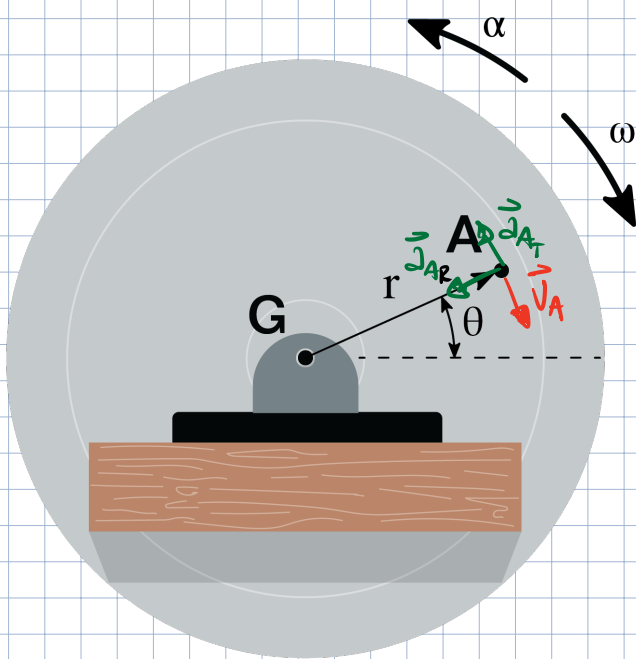


A disk is rotating with an angular velocity $\omega = 2 \text{ rad/s}$ and angular acceleration $\alpha = 1 \text{ rad/s}^2$. Determine the velocity and acceleration of point A, located a distance $r = 1 \text{ m}$ from the center of the disk at a 30° angle from the horizontal ($\theta = 30^\circ$).



$$\vec{r} = r \cos \theta \hat{i} + r \sin \theta \hat{j}$$

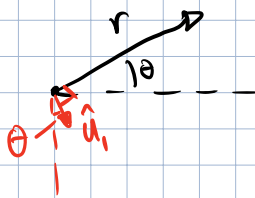
$$\vec{v}_A = \vec{v}_G + \vec{\omega} \times \vec{r}$$

$$\vec{v}_A = \vec{\omega} \times \vec{r} = (-2 \text{ rad/s } \hat{k}) \times 1 \text{ m} (\cos 30^\circ \hat{i} + \sin 30^\circ \hat{j})$$

$$\vec{v} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 0 & -2 \\ \cos 30^\circ & \sin 30^\circ & 0 \end{vmatrix} = 2 \sin 30^\circ \hat{i} - 2 \cos 30^\circ \hat{j}$$

$$\vec{v}_A = 1 \hat{i} - 1.73 \hat{j} \text{ m/s}$$

$$|\vec{v}_A| = |\vec{\omega}| |\vec{r}| = (2 \text{ rad/s})(1 \text{ m}) = 2 \text{ m/s}$$



$$\hat{u}_1 = \sin \theta \hat{i} - \cos \theta \hat{j}$$

$$\vec{v}_A = |\vec{v}_A| \hat{u}_1 = (2 \text{ m/s}) (\sin 30^\circ \hat{i} - \cos 30^\circ \hat{j}) = 1 \hat{i} - 1.73 \hat{j} \text{ m/s}$$

$$\vec{a} = \vec{\alpha} \times \vec{r} - \omega^2 \vec{r} = (1 \text{ rad/s}^2 \hat{k}) \times 1 \text{ m} (\cos 30^\circ \hat{i} + \sin 30^\circ \hat{j}) - (2 \text{ rad/s})^2 1 \text{ m} (\cos 30^\circ \hat{i} + \sin 30^\circ \hat{j})$$

$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 0 & 1 \\ \cos 30^\circ & \sin 30^\circ & 0 \end{vmatrix} - 4 \cos 30^\circ \hat{i} - 4 \sin 30^\circ \hat{j}$$

$$= -\sin 30^\circ \hat{i} + \cos 30^\circ \hat{j} - 4 \cos 30^\circ \hat{i} - 4 \sin 30^\circ \hat{j}$$

$$= -5 \sin 30^\circ \hat{i} + 5 \cos 30^\circ \hat{j}$$

$$\vec{a} = -2.5 \hat{i} + 4.3 \hat{j} \text{ m/s}^2$$